



Article

## Computational Simulation of the Lotka–Volterra Predator–Prey Model

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**Abstract:** Ecological theory has long held that predator-prey dynamics drive oscillations between resource and consumer populations (hereafter, the predator-prey relationship). A classical Lotka–Volterra model was modified to represent the impacts of an oscillatory environment with sufficient seasonal forcing to maintain stability and homeostasis at the scale of the system, and to provide a dynamic home for examination of oscillatory dynamics and system stability. The study allows for the explicit display of trajectories of populations by using advanced numerical methods to accurately solve a constellation of nonlinear differential equations. The temporal evolution of simulation data shows a constant cycle of oscillation where the predator population rises from a phase lag relative to the background response in combination with a surge in prey density. In fact, as highlighted at the end of the citation we just provided, the fact that computer modeling is an important part of identifying regulatory mechanisms behind population cycles does not mean that it will not be an important part of the process going forward. In addition, the generality of this framework permits its deployment with a full simulation environment for various real-world scenarios — from wildlife conservation and agricultural pest control, to more abstract activities models of research intervention, such as epidemic and treatment strategies.

**Keywords:** Predator–prey dynamics; Lotka–Volterra model; Mathematical modeling; Numerical simulation; Stability analysis; Ecological resilience; Computational methods

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### 1. Introduction

Predator–prey interactions are an essential force structuring ecological communities and underlie the operation of all ecological systems. The Lotka–Volterra model[3] is a pair of first-order, nonlinear, differential equations frequently used to describe the dynamics of population growth of species in a community, originally formalised in the 1920s. Computational models are one of the most powerful forms of experimental approaches, providing a complementary avenue to study how models behave with more complexity added such as heterogeneity, stochastic effects, or multi-agent modes of interaction or feedback. These, however, are not just abstract concepts, as dynamics are essential for stability, biodiversity and resilience, and help establish the health and sustainability of natural systems in the long-term. Based on classical literature, i.e., the Lotka–Volterra equations [1], an emerging framework for the complexity of mechanisms that drive species interactions between organisms (also called multi-species) is the trophic (predation or competition related) assemblage [18,19]. These progresses not only mark the chain of species and, more importantly, reinforces the capacity to change the outcome of this change (the cycle of the species) The abundance of prey for mammals cats stimulates an increase in the population of the cats through prey predation pressure, this will then be above the level that will allow the populations of prey to sustain themselves. It is this feedback loop the interaction of the principles of respect for fragility and the dynamics

within circles of governance that the cyclical nature of these principles are mathematically defined as producing.

## 2. Materials and Methods

- Geometric and Dynamical Analysis:
  - a. State Space (Phase Space): The relationship between mortality and reproduction rates in closed provinces when represented as a state. This implies that the system has a central feeding point, which explains why species do not graze in this model despite the presence of harmful barriers.
  - b. Limitations of the "critical effect": Despite the explanatory power of the Lotka-Volterra model, the next generation is expected to be unimpeded. In this model, these equations have been modified to include "total capacity" (endurance), where the decline in prey is not limited to fungi but also includes resource constraints, thus transforming the mechanisms into stable loops.

Ecological models of the contemporary leap have seen a timescale beyond traditional frameworks, incorporating familiar changes that introduce necessary risk factors, such as time delays, permanent impacts on attractive prey habitats, and overlapping disease dynamics [2]. These expansions not only enrich the limited description but also remove contingent constraints (emerging behaviors) that were not present in the assemblages, such as dendrites and disordered systems. For example, these serve as reference points for researchers seeking to analyze and select parameters (parameter sensitivity). Thus, the analysis of the evolutionary schema [3] (planar phase analysis) and wind-driven dendrite movement provides a future view of system stability and continuity, helping to predict conditions that will promote coexistence and sustainability or species collapse. Similarly to the change in the diffusion rate values, the shift from stable periodic mechanisms to spatiotemporal chaos of electronics indicates the degree of global cooperation to solve the international problems or the climate change[6]. In addition, the apparent cluster of "safe havens" serving as a wheelchair that persist on the extinction threshold bubble on despite only effective predators, renders the core function of safe havens essential as well, With the central role of modelling transcending its role as tool for simulation, propagating also to its construction as one of the cornerstones of environmental and applied science [4, 6]. Offers the necessary logical content for realizing couplings between both very complex ecological and biological systems. Scientists convert biological interactions, such as predator-prey relationships and concurrency for resources, into quantitative equations to investigate the mechanisms maintaining and regulating these systems, and to forecast how they will behave moving forward. Collectively these models enables scientists to examine theoretical hypotheses and provide scenario templates that may be difficult to empirically investigate because of logistical or ethical reasons [7-11], and may help to identify threshold points along a continuum pathway between stable and collapsed states of a system. This tactic has interesting consequences in further domains – (predicting) the outbreak of diseases, inter-economy rivalry, ecosystems and climate stability. As an intermediate between frameworks and application, modeling has a role to play in the rapid dissemination of scientific progress, but also in environments in which scientific knowledge must underpin public policy, conservation and natural resource management in the face of systems that are usually better specified in the abstract [12].

Predator-prey dynamics are fundamental to theory in ecology and solving these and similar puzzles can help to inform management of predators and prey, environmental planning, and even systems with similar consumer-supplier relationships, such as epidemiology and economics. In this regard, this study seeks to simulate and analyze the predator-prey system using advanced computational methodologies, with a particular focus on how changes in conversion efficiency and mortality rates affect the stability of the system as a whole and the sustainability of species.

## 3. Results and Discussion

Mathematical Formula:

Consider an ecosystem with two species  $(N_1, N_2)$  s.t. the rate of change of each species depend only on the populations of both species i.e.:

$$\frac{dN_1}{dt} = f_1(N_1, N_2) \quad (1)$$

$$\frac{dN_2}{dt} = f_2(N_1, N_2) \quad (2)$$

Now we can translate this principle into a Mathematical model, the classical Lotka-Volterra is will be written as [13]:

$$\frac{\partial x}{\partial t} = \alpha x - \beta xy \quad (3)$$

$$\frac{\partial y}{\partial t} = \delta xy - \gamma y \quad (4)$$

Where,  $x(t)$  is the prey population,  $y(t)$  is predator population,  $\alpha$  is prey growth rate,  $\beta$  is predation rate,  $\gamma$  is predator mortality rate and  $\delta$  is predator reproduction rate see figure (1). The equilibrium occurs when both derivatives equal zero, leading to nontrivial steady states.

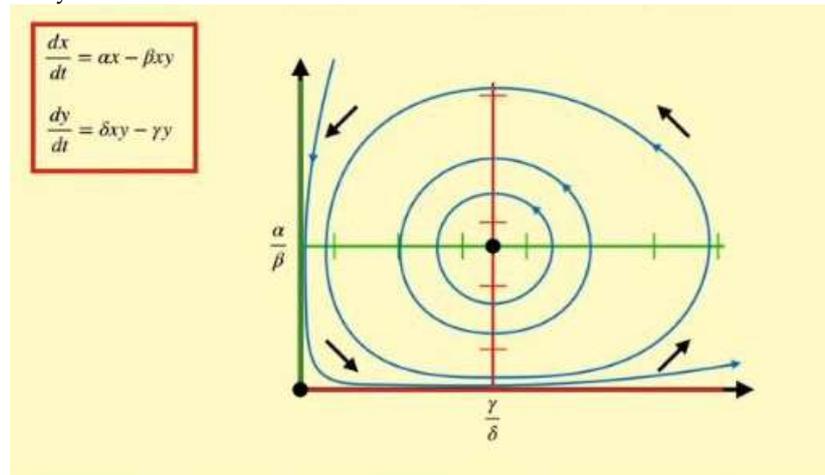


Figure 1. shows the relationship between the prey and predator.

Now, if we want to solve the eq.s 3 and 4 we get:

$$\frac{\partial x}{\partial t} = x(\alpha - \beta y) = 0 \quad (5)$$

$$\frac{\partial y}{\partial t} = y(\delta x - \gamma) = 0 \quad (6)$$

$$x = 0, y = 0 \Rightarrow E_0 = (0, 0) \quad (7)$$

$$y = \frac{\alpha}{\beta}, \text{ put in (6) we get } x = \frac{\gamma}{\delta} \Rightarrow E_1 = \left(\frac{\gamma}{\delta}, \frac{\alpha}{\beta}\right) \quad (8)$$

$$J(x, y) = \begin{pmatrix} \alpha - \beta y & -\beta x \\ \delta y & \gamma - \delta x \end{pmatrix} \quad (9)$$

$$J(0, 0) = \begin{pmatrix} \alpha & 0 \\ 0 & \gamma \end{pmatrix} \quad (10)$$

$$|A - \lambda I| = 0 \Rightarrow \lambda_1 > 0, \lambda_2 > 0 \text{ so } (0, 0) \text{ is unstable node, see figure 2} \quad (11)$$

$$J\left(\frac{\alpha}{\beta}, \frac{\gamma}{\delta}\right) = \begin{pmatrix} 0 & -\alpha \\ -\gamma & 0 \end{pmatrix} \quad (12)$$

$$|A - \lambda I| = 0 \Rightarrow \lambda_{1,2} = \pm \sqrt{\alpha\gamma}, \text{ so } \left(\frac{\alpha}{\beta}, \frac{\gamma}{\delta}\right) \text{ is unstable saddle point, see figure 3} \quad (13)$$

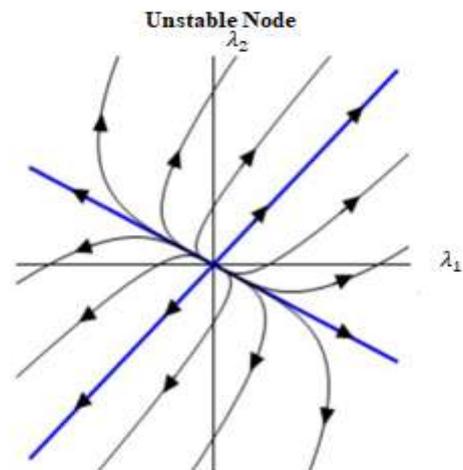


Figure 2. shows the strategy of Nod point.

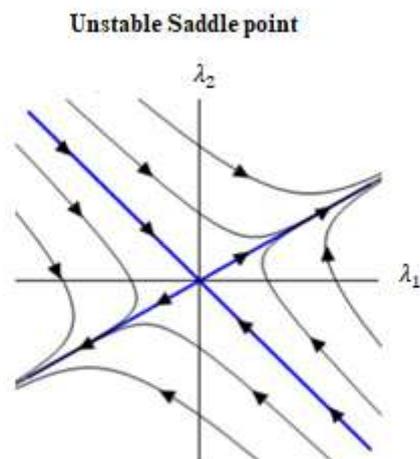


Figure 3. shows the strategy of Saddle point.

If we take, for example, the following research [14], " Alternative Stochastic Modeling to Lotka-Volterra using a Multi-Agent System" , to study how computer simulations are used in research, we will notice that the differential equations were solved numerically, the eigenvalues and eigenvectors for each value were found, and the dynamic behavior of each value and its relationship to the given mathematical model [15] were studied. Therefore, we observe that the simulation results, derived from specific parameters and initial conditions, are summarized in Matlab program, the multi-agent system's behavior is detailed in Figure 4. Specifically, Figure 4a tracks the temporal evolution of both populations, highlighting oscillatory dynamics with a reproductive period of approximately 50 cycles and prey peaks recurring every ~300 cycles. A distinct phase lag and coupled oscillations between prey and predator are clearly visible. Figure 4b illustrates the system's phase-space trajectory, juxtaposing the stochastic multi-agent results with the deterministic Lotka Volterra prediction using  $\alpha = 0.2, \beta = 0.27, \gamma = 0.9, \delta = 0.05$ . This well-defined green closed orbit common for deterministic models stands in stark contrast to the random oscillations produced by a stochastic simulation. The transition in the temporal evolution of biomass is evident when we use a box-and-whisker plot of population size (figure 4c), while in the box-and-whisker plot of a phase-space plot (figure 4d), the cycles are also visible in total biomass due to the nature of

depletion of resources integrated over multi-trophic interactions (predator-prey dynamics).

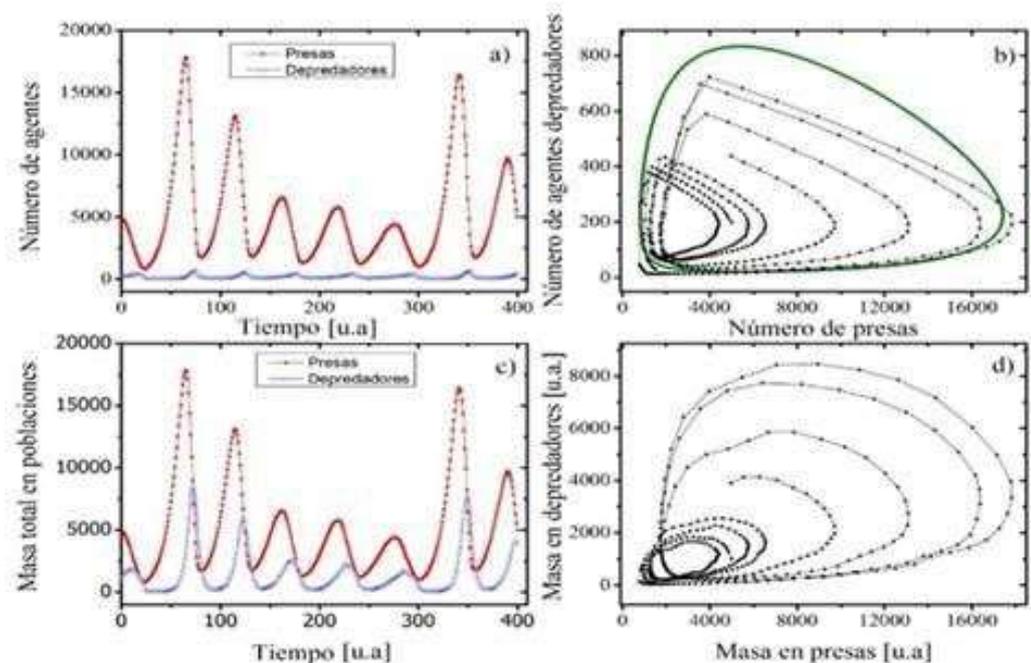


Figure 4. show the simulation of Lotka- Voletar modul.

#### 4. Conclusion

This computational study shows that we can study the cyclical behavior of ecological interactions using a mathematical model, because these cycles especially the nonlinear and complex ones do not lend themselves easily to a peak and trough investigation. One of the hallmarks of classical predator-prey dynamics with phase-lag structure is the identification of prey abundance leading to peaks in predators a fixed time later, as shown by analyses of series in time. The closed orbits testify for two always positives populations and the trajectories in the phase plane prove these oscillations but at this equilibrium state is definitely unstable. In fact sensitivity analyses reveal just how sensitively the system responds to initial conditions a small difference in growth or death rates can lead to local extinction or chaotic destabilization of the two populations.

A significant portion of this work consists of many nearly-analytically unsolvable nonlinear differential equations solvable exclusively with an automated numerical set-up (see Methods). MATLAB and Python and Mathematica are great for this because in addition to being able to solve the equations, you can also quickly dumb down complicated models that are repeatable. They enable us to seamlessly integrate the most theoretical parts of mathematics advanced calculus in conjunction with numerical computations with applied ecological management, allowing us to create complex simulations with minimal effort. Ecosystem resilience may be more easily quantified through simulation of elevated, current, immediate stressors at multiple ecological levels. Moreover, the prediction expertise of those algorithmic tools for the same factor transcend ecology, suggesting methods to control epidemics and modulate financial system volatility as effectively.

##### Future Research Trajectories

From the facts outlined here, we propose the following general approaches to increase the ecological realism of the Lotka-Volterra formulation:

1. Multitrophic complexity at the dyad level Although key interactions are represented via the classic predator-prey dyad, the model should be extended to compose multi-species food webs. This method provides a representation that is more consistent

with the complexity of natural systems through the consideration of indirect interactions (e.g., apparent competition and trophic cascades)..

2. Given that biological interactions and environmental variables are fundamentally unpredictable, this might simply be stated as a critique suggesting that future models should be generically stochastic in formulation, not strictly deterministically. To derive the probability of extinction and predict population persistence over long time scales when faced with environmental perturbation, variability in birth and death rates must be incorporated.

3. More realistic models that include spatial dynamics (e.g. migration corridors and environmental heterogeneity) can enhance spatial approaches (habitat fragmentation and conservation). This directly assists landscape-scale conservation planning, and facilitates a much broader evaluation on the effect of habitat fragmentation and the configuration of the landscape on resilience and stability of the predator-prey cycle.

4. Ultimately, we need to test every theoretical model against data and use the observational parameters to constrain it. While spatially explicit predator-prey models have the potential to rapidly translate ecological theory into applied wildlife management and policy predictions, this ability is limited until realistic estimates of search rates and handling times can be developed at the scale of interest.

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